

# Class 4: debt overhang

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The lectures on debt overhang stress the difficulties of renegotiation; this problem set follows ★ Myers (1977) in emphasising the interests in which the firm acts.

Consider a two period world in which a firm first chooses a capital structure. There are  $N$  possible states of the economy in the future,  $s_1, \dots, s_N$ , with the  $n^{\text{th}}$  expected to arise with probability  $\pi_n$ . Once the firm's managers learn which state occurs, they decide whether or not to undertake an investment. The investment costs  $I$  to undertake, and yields return  $R(s_n)$  in state  $s_n$ , with states ranked so that  $R(s_1) < \dots < R(s_n) < \dots < R(s_N)$ . The firm has no other assets; there are no taxes or transactions costs; there are no agency costs, meaning that managers implement shareholders' wishes.

1. What is the efficient investment rule?
2. Suppose first that the firm initially raised  $I$  via equity financing.
  - (a) What investment rule do the shareholders instruct management to adopt? Denote the least profitable state in which the shareholders agree to invest by  $s_a$ .
  - (b) What is the expected value of the equity-financed firm initially?
3. Now suppose that the firm initially issued a mix of debt and equity to raise  $I$ , and that  $D$  must be repaid.

- (a) What investment rule do the shareholders instruct management to adopt? Denote the least profitable state in which the shareholders agree to invest by  $s_b$ .
- (b) What is the expected value of the equity-financed firm initially?

#### 4. Optimal capital structure

- (a) Which capital structure maximises the value of the firm?
- (b) Comment on what happens in states  $s_a, \dots, s_{b-1}$ .
- (c) What might debtholders try to do in states  $s_a, \dots, s_{b-1}$ ? Why might this not be possible?

## References

- S. C. Myers. Determinants of corporate borrowing. *Journal of Financial Economics*, 5(2):147 – 175, November 1977.